

Name: _____ Date: _____ Block: _____ # _____

Quarter 2 Benchmark Review

1. Sketch each function. Complete the chart with the required information.

a) $f(x) = x^2(x-1)$

Leading Coefficient: 1	Degree: x^3 Cubic
End Behavior: $\downarrow \uparrow$	
Zeros (list multiplicity in parentheses)	Rough sketch of graph:
$x = 0$ (mult of 2)	
$x = 1$	

b) $f(x) = -x(x-1)(x+2)$

Leading Coefficient: -1	Degree: x^3 Cubic
End Behavior: $\uparrow \downarrow$	
Zeros (list multiplicity in parentheses)	Rough sketch of graph:
$x = 0$	
$x = 1$	
$x = -2$	

c) $f(x) = x(x+4)(x-1)^2$

Leading Coefficient: 1	Degree: x^4 Quartic
End Behavior: $\uparrow \uparrow$	
Zeros (list multiplicity in parentheses)	Rough sketch of graph:
$x = 0$	
$x = -4$	
$x = 1$ (mult of 2)	

3) Given one zero find all the zeros:

a) $f(x) = 9x^3 + 10x^2 - 17x - 2; -2$

$$\begin{array}{r|rrrr} -2 & 9 & 10 & -17 & -2 \\ & \downarrow & -18 & +16 & 2 \\ \hline & 9 & -8 & -1 & 0 \end{array}$$

$$9x^2 - 8x - 1 = 0$$

$$(9x + 1)(x - 1) = 0$$

$x = -\frac{1}{9}$	$x = 1$	$x = -2$
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b) $f(x) = x^3 - 14x^2 + 47x - 18; 9$

$$\begin{array}{r|rrrr} 9 & 1 & -14 & 47 & -18 \\ & \downarrow & 9 & -45 & 18 \\ \hline & 1 & -5 & 2 & 0 \end{array}$$

$$x^2 - 5x + 2 = 0$$

$a = 1$
 $b = -5$
 $c = 2$

$$x = \frac{5 \pm \sqrt{(-5)^2 - 4(1)(2)}}{2(1)}$$

$x = \frac{5 \pm \sqrt{17}}{2}$	$x = 9$
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Given one zero find all the zeros:

c) $f(x) = x^3 + x^2 + 2x + 24; -3$

$$\begin{array}{r|rrrr} -3 & 1 & 1 & 2 & 24 \\ & \downarrow & -3 & 6 & -24 \\ \hline & 1 & -2 & 8 & 0 \end{array}$$

$$x^2 - 2x + 8 = 0$$

$$\begin{aligned} a &= 1 \\ b &= -2 \\ c &= 8 \end{aligned}$$

$$x = \frac{2 \pm \sqrt{(-2)^2 - 4(1)(8)}}{2(1)}$$

$$x = \frac{2 \pm \sqrt{-28}}{2}$$

$$x = \frac{2 \pm \sqrt{-1} \sqrt{4} \sqrt{7}}{2}$$

$$x = \frac{2 \pm 2i\sqrt{7}}{2}$$

$$x = 1 \pm i\sqrt{7} \quad | \quad x = -3$$

- 4) In a test kitchen, researchers have measured the radius of a ball of dough made with a new quick-acting yeast. Based on their data, the radius r of the dough ball, in centimeters, is given by $r = 5(1.05)^{\frac{t}{3}}$ after t minutes. Round the answers to the following questions to the nearest tenth of a cm.

- a. What is the radius after 5 minutes?

$$r = 5(1.05)^{\frac{5}{3}}$$

$$r = 5.4 \text{ cm}$$

- b. What is the radius after 20 minutes?

$$r = 5(1.05)^{\frac{20}{3}}$$

$$r = 6.9 \text{ cm}$$

- c. What is the radius after 43 minutes?

$$r = 5(1.05)^{\frac{43}{3}}$$

$$r = 10.1 \text{ cm}$$

- 5) Simplify:

$$\sqrt[3]{63} + 4\sqrt[3]{9}$$

a) $4\sqrt[3]{81} + 2\sqrt[3]{72} - 3\sqrt[3]{24}$

$$\begin{aligned} &4\sqrt[3]{27 \cdot 3} + 2\sqrt[3]{8 \cdot 9} - 3\sqrt[3]{8 \cdot 3} \\ &4 \cdot 3\sqrt[3]{3} + 2 \cdot 2\sqrt[3]{9} - 3 \cdot 2\sqrt[3]{3} \\ &12\sqrt[3]{3} + 4\sqrt[3]{9} - 6\sqrt[3]{3} \end{aligned}$$

b) $\sqrt{28} + 4\sqrt{63} - 2\sqrt{7}$

$$\begin{aligned} &\sqrt{4 \cdot 7} + 4\sqrt{9 \cdot 7} - 2\sqrt{7} \\ &2\sqrt{7} + 4 \cdot 3\sqrt{7} - 2\sqrt{7} \\ &12\sqrt{7} \end{aligned}$$